Econometrics I

Lecture 5: Extended Example: The Wage Equation

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Fall 2018

Preliminaries

- I'm posting problem set solutions and grades on NYU Classes.
- Start thinking about your group project groups and topics, if you haven't already! I will distribute some topic suggestions by next week's lecture.

Mincerian Regression

• Recall the Mincerian regression (wage equation):

$$\label{eq:loss_equation} \mbox{In wage}_i = \beta_0 + \beta_{ed} \mbox{Edu}_i + \beta_{exp} \mbox{Exp}_i + \beta_{Fem} \mbox{Fem}_i + \dots + \varepsilon_i$$

• Let's revisit estimating this with the Cornwell and Rupert data.

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Baseline Results

```
> suppressMessages(library(tidyverse))
Worning messages:
1: package 'tibble' was built under R version 3.4.4
2: package 'tidyr' was built under R version 3.4.4
3: package 'purrr' was built under R version 3.4.4
4: package 'purrr' was built under R version 3.4.3
> datod - read.csv('cornwell-rupert.csv')
> #data - cbind(data, EXP2-data5EXPA2)
> data - data %% mutate(EXP2 = EXPA2)
> reg_1 - lm(LWAGE - ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA + MS + FEM + UNION, data = data)
> summary(reg_1)
```

```
Call:
lm(formula = LWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA +
   MS + FEM + UNION, data = data)
Residuals:
   Min
            10 Median
-2.2034 -0.2379 -0.0071 0.2327 2.1380
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.245e+00 7.170e-02 73.153 < 2e-16 ***
ED
            5.654e-02 2.612e-03 21.644 < 2e-16 ***
EXP
            4.045e-02 2.174e-03 18.605 < 2e-16 ***
FXP2
           -6.811e-04 4.783e-05 -14.242 < 2e-16 ***
WKS
            4.485e-03 1.090e-03 4.115 3.94e-05 ***
OCC
           -1.405e-01 1.472e-02 -9.544 < 2e-16 ***
SOUTH
           -7 210e-02 1 249e-02 -5 773 8 37e-09 ***
SMSA
            1.390e-01 1.207e-02 11.513 < 2e-16 ***
MS
            6.736e-02 2.063e-02 3.265 0.0011 **
FFM
           -3.892e-01 2.518e-02 -15.457 < 2e-16 ***
UNTON
            9.015e-02 1.289e-02 6.993 3.13e-12 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.3524 on 4154 degrees of freedom Multiple R-squared: 0.4183, Adjusted R-squared: 0.4169 F-statistic: 298.7 on 10 and 4154 DF, p-value: < 2.2e-16

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Relaxing Linear Effect of Education

```
> data <- data %5% mutate(NORS = ifelse(ED <- 8, 1, 0),
+ SOMENS = ifelse(ED >= 10) & (ED <= 11), 1, 0),
+ SOMECOL = ifelse(ED >= 13) & (ED <= 11), 1, 0),
+ SOMECOL = ifelse(ED >= 13) & (ED <= 15), 1, 0),
+ OL = ifelse(ED >= 13) & (ED <= 15), 1, 0),
+ POST = ifelse(ED >= 17, 1, 0)
+ Otto = ifelse(ED >= 17, 1, 0)
+ SOMECOL + OL + POST)
- reg. 2 <- lm(LNAGE = NONS + SOMECOL + COL + POST)
- reg. 2 <- lm(LNAGE = NONS + SOMECOL + COL + POST) + EXP + EXP = INV2 = NWS + OCH + SOUTH + SMSA
+ MS + FEM + UNION, data = data)
> summary(reg. 2)
```

 Note that we're missing a coefficient on one of the education categories.

```
Coefficients: (1 not defined because of singularities)
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 6.188e+00 5.888e-02 105.112 < 2e-16 ***
NOHS
           -5.337e-01 2.947e-02 -18.108 < 2e-16 ***
SOMEHS
           -3.937e-01 2.496e-02 -15.776 < 2e-16 ***
           -2.855e-01 2.106e-02 -13.554 < 2e-16 ***
SOMECOL
           -1.973e-01 2.214e-02 -8.912 < 2e-16 ***
           -2.711e-02 2.127e-02 -1.274 0.202570
COL
POST
FXP
            4.100e-02 2.184e-03 18.769 < 2e-16 ***
EXP2
           -6.940e-04 4.799e-05 -14.461 < 2e-16 ***
WKS
            4.599e-03 1.103e-03 4.168 3.14e-05 ***
           -1.386e-01 1.509e-02 -9.184 < 2e-16 ***
occ
SOUTH
           -7.618e-02 1.259e-02 -6.052 1.56e-09 ***
SMSA
            1.436e-01 1.211e-02 11.861 < 2e-16 ***
MS
            6.919e-02 2.070e-02 3.343 0.000837 ***
           -3.819e-01 2.532e-02 -15.080 < 2e-16 ***
            9 402e-02 1 300e-02 7 235 5 52e-13 ***
LINTON
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.3529 on 4150 degrees of freedom Multiple R-squared: 0.4174, Adjusted R-squared: 0.4154 F-statistic: 212.4 on 14 and 4150 DF, p-value: < 2.2e-16

Dropping a Category Dummy

```
> # regression with categories, dropping one
> reg_3 < lm(LMAGE ~ SOMEHS + HS + SOMECOL + COL
+ POST + EXP + EXP2 + WKS + DCC + SOUTH + SMSA
+ MS + FEM + UNION, data = data)
> summary(reg_3)
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.655e+00 6.342e-02 89.170 < 2e-16 ***
SOMEHS
            1.400e-01 2.485e-02 5.632 1.90e-08 ***
HS
            2.482e-01 2.292e-02 10.827 < 2e-16 ***
SOMECOL
            3.364e-01 2.679e-02 12.555 < 2e-16 ***
COL
            5.066e-01 2.835e-02 17.868 < 2e-16 ***
POST
            5.337e-01 2.947e-02 18.108 < 2e-16 ***
EXP
           4.100e-02 2.184e-03 18.769 < 2e-16 ***
           -6.940e-04 4.799e-05 -14.461 < 2e-16 ***
FXP2
WKS
           4.599e-03 1.103e-03 4.168 3.14e-05 ***
OCC
           -1 386e-01 1 509e-02 -9 184 < 2e-16 ***
           -7.618e-02 1.259e-02 -6.052 1.56e-09 ***
SOUTH
SMSA
           1.436e-01 1.211e-02 11.861 < 2e-16 ***
MS
            6.919e-02 2.070e-02 3.343 0.000837 ***
FEM
           -3.819e-01 2.532e-02 -15.080 < 2e-16 ***
UNION
            9.402e-02 1.300e-02 7.235 5.52e-13 ***
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.3529 on 4150 degrees of freedom Multiple R-squared: 0.4174, Adjusted R-squared: 0.4154 F-statistic: 212.4 on 14 and 4150 DF, p-value: < 2.2e-16

Dropping the Constant Term

```
> reg_4 <- lm(LWAGE ~ NOHS + SOMEHS + HS + SOMECOL + COL
+ POST + EXP + EXP2 + NKS + OCC + SOUTH + SMSA
+ HS + FEM + UNION -1, data = data)
> summary(reg_4)
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
NOHS
        5.655e+00 6.342e-02 89.170 < 2e-16 ***
SOMEHS 5.795e+00 6.240e-02 92.864 < 2e-16 ***
        5.903e+00 6.095e-02 96.855 < 2e-16 ***
SOMECOL 5.991e+00 6.096e-02 98.276 < 2e-16 ***
        6.161e+00 5.966e-02 103.268 < 2e-16 ***
POST
        6.188e+00 5.888e-02 105.112 < 2e-16 ***
        4.100e-02 2.184e-03 18.769 < 2e-16 ***
EXP2
       -6.940e-04 4.799e-05 -14.461 < 2e-16 ***
WKS
        4.599e-03 1.103e-03 4.168 3.14e-05 ***
000
       -1.386e-01 1.509e-02 -9.184 < 2e-16 ***
SOUTH
       -7.618e-02 1.259e-02 -6.052 1.56e-09 ***
SMSA
       1.436e-01 1.211e-02 11.861 < 2e-16 ***
        6.919e-02 2.070e-02 3.343 0.000837 ***
       -3.819e-01 2.532e-02 -15.080 < 2e-16 ***
        9.402e-02 1.300e-02 7.235 5.52e-13 ***
LINTON
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3529 on 4150 degrees of freedom Multiple R-squared: 0.9972, Adjusted R-squared: 0.9972 F-statistic: 9.96e+04 on 15 and 4150 DF, p-value: < 2.2e-16

Two Ways of Testing Hypotheses

```
> suppressMessages(library(sandwich))
> # separate male and female categories
> data <- data %>% mutate(MALE = ifelse(FEM == 1, 0, 1))
> reg_5 <- lm(LWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
             + MS + FEM + MALE + UNION -1, data = data)
> linearHypothesis(rea_5, c("FEM = MALE"),
                  vcov = vcovHC(reg_5, type = "HC1"))
Linear hypothesis test
Hypothesis:
FEM - MALE = 0
Model 1: restricted model
Model 2: LWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA + MS + FEM +
   MALE + UNTON - 1
Note: Coefficient covariance matrix supplied.
  Res.Df Df
                F Pr(>F)
1 4155
2 4154 1 263.33 < 2.2e-16 ***
Signif, codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
> # now with intercept and different (but equivalent) hypothesis test
> data <- data %>% mutate(MALE = ifelse(FEM == 1, 0, 1))
> reg 6 <- lmCLWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
             + MS + FEM + UNION , data = data)
> linearHypothesis(rea 6, c("FEM = 0"), vcov = vcovHC(rea 6, type = "HC1"))
Linear hypothesis test
Hypothesis:
FFM - 0
Model 1: restricted model
Model 2: LWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA + MS + FEM +
   UNTON
Note: Coefficient covariance matrix supplied.
 Res.Df Df
                F Pr(>F)
1 4155
2 4154 1 263.33 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

> suppressMessages(library(car))

Delta Method I

- We know how to compute standard errors on our coefficients, but sometimes we are interested in functions of those statistics
- For example, if we have linear and quadratic terms of experience $(\beta_{exp}Exp_i + \beta_{exp2}Exp_i^2)$, then the model doesn't just have a simple "effect of experience".
- We might be interested in the effect of experience for somebody with 10 years of experience:

$$\frac{d \ln Wage_i}{dExp_i} \bigg|_{Exp_i = 10} = \beta_{exp} + 2\beta_{exp2}exp_i = \beta_{exp} + 20\beta_{exp2}$$

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Delta Method II

Suppose we have an asymptotic distribution for an estimator:

$$\sqrt{n}(\mathbf{b}-\boldsymbol{\beta}) \Rightarrow_d \mathcal{N}(\mathbf{0}, \boldsymbol{\Sigma}).$$

• Then the asymptotic distribution of a function of the estimator is

$$\sqrt{n}\left(g\left(\mathbf{b}\right)-g\left(\boldsymbol{\beta}\right)\right)\Rightarrow_{d}\mathcal{N}\left(\mathbf{0},\left(\nabla g\left(\boldsymbol{\beta}\right)\right)'\mathbf{\Sigma}\nabla g\left(\boldsymbol{\beta}\right)\right)$$
,

where $\nabla g(\beta)$ is the gradient of $g(\beta)$:

$$abla g\left(oldsymbol{eta}
ight) = \left(egin{array}{c} rac{\partial g\left(oldsymbol{eta}
ight)}{\partialeta_{1}} \ rac{\partial g\left(oldsymbol{eta}
ight)}{\partialeta_{2}} \ dots \ rac{\partial g\left(oldsymbol{eta}
ight)}{\partialeta_{k}} \end{array}
ight).$$

• Note that we can estimate $\nabla g(\beta)$ with $\nabla g(\mathbf{b})$.

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Delta Method in R

Numerical Bootstrap

Given the the asymptotic distribution of a parameter estimate

$$\mathbf{b}\sim_{d}\mathcal{N}\left(oldsymbol{eta},oldsymbol{\Sigma}
ight)$$
 ,

we have an estimated density function \hat{f} . Let \hat{f} be the multivariate normal density with mean β and variance Σ .

- ullet We can simulate the asymptotic distribution of $g(\mathbf{b})$ by
 - ▶ Simulating draws \mathbf{b}_m for m = 1, 2, ... M from \hat{f}
 - Computing $g(\mathbf{b}_m)$ for each draw
 - ► Then $(g(\mathbf{b}_1), g(\mathbf{b}_2), \dots, g(\mathbf{b}_M))$ will be a simulated asymptotic distribution for
- This can be useful when you have code to compute $g(\cdot)$, but computing the derivative $g(\cdot)$ would be difficult. For example, when $g(\cdot)$ represents an complex behavioral (or equilibrium) model.

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Heterogeneous Effects

When we have a model of the form

$$Y_i = \beta_0 + \beta_1 X_{1i} + \varepsilon_i$$

we're implicitly saying that the effect of X_1 is the same for all individuals.

- Often we would like to relax this, allowing different groups to have different slopes with respect to X_1 .
- This is easy as long as the group membership is observed in the data. We simply interact the regressor with dummy variables:

$$Y_i = \beta_0 + \beta_{0F} D_{Fi} + \beta_1 X_{1i} + \beta_2 X_{1i} D_{Fi} + \varepsilon_i$$

where D_{Fi} is a dummy variable for whether individual i is female. Note that we have allowed for the intercepts and slopes to vary by sex here.

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Heterogeneous Effects in R

```
> data <- cbind(data, EDFEM-dataSED*dataSFEM)
> reg_9 <- lm(LWAGE ~ ED + EDFEM + EXP + EXP2 + WKS + OCC + SOUTH + SMSA + MS + FEM + UNION, data = data)
> summarv(reg_9)
```

- Here, we construct interactions manually, allowing education to have a different effect for males and females.
- Does education have significantly different effects for males and females?

```
Call:
lm(formula = LWAGE ~ ED + EDFEM + EXP + EXP2 + WKS + OCC + SOUTH
SMSA + MS + FEM + UNION, data = data)
```

```
Residuals:
Min 1Q Median 3Q Max
-2.19425 -0.23540 -0.00569 0.23005 2.13574
```

8.476e-02 1.296e-02

Coefficients: Estimate Std. Error t value Pr(>|t|) (Intercept) 5.277e+00 7.212e-02 73.173 < 2e-16 *** 5.413e-02 2.689e-03 20.126 < 2e-16 EDEEM 6.868e-03 3.669 0.000246 EXP 4.053e-02 2.171e-03 18.668 < 2e-16 FXP2 -6.842e-04 4.776e-05 -14.324 < 2e-16 *** WKS 4.518e-03 1.088e-03 4.151 3.37e-05 *** occ -1.383e-01 1.472e-02 -9.396 < 2e-16 *** SOUTH -7.375e-02 1.248e-02 -5.910 3.70e-09 1.402e-01 1.206e-02 11.626 < 2e-16 SMSA MS 6.539e-02 2.061e-02 3.173 0.001520 ** FFM -7 153e-01 9 235e-02 -7 745 1 19e-14 ***

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.3519 on 4153 degrees of freedom Multiple R-squared: 0.4201, Adjusted R-squared: 0.4186 F-statistic: 273.5 on 11 and 4153 DF, p-value: < 2.2e-16

6.542 6.81e-11 ***

UNION

Interactions with the : Operator

```
> reg_10 <- lm(LWAGE ~ ED + ED:FEM + EXP + EXP2 + WKS + OCC + SOUTH + SMSA + + MS + FEM + UNION, data = data) > summarv(rea.10)
```

 We can avoid creating the interactions mandually with the : operator.

```
Call:
lm(formula = LWAGE ~ ED + ED:FEM + EXP + EXP2 + WKS + OCC + SOUTH +
   SMSA + MS + FEM + UNION, data = data)
Residuals:
    Min
              10 Median
-2.19425 -0.23540 -0.00569 0.23005 2.13574
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.277e+00 7.212e-02 73.173 < 2e-16 ***
            5.413e-02 2.689e-03 20.126 < 2e-16 ***
ED
EXP
            4.053e-02 2.171e-03 18.668 < 2e-16 ***
           -6.842e-04 4.776e-05 -14.324 < 2e-16 ***
EXP2
WKS
            4.518e-03 1.088e-03 4.151 3.37e-05 ***
OCC
           -1.383e-01 1.472e-02 -9.396 < 2e-16 ***
SOUTH
           -7.375e-02 1.248e-02 -5.910 3.70e-09 ***
SMSA
            1.402e-01 1.206e-02 11.626 < 2e-16 ***
            6.539e-02 2.061e-02 3.173 0.001520 **
FEM
           -7.153e-01 9.235e-02 -7.745 1.19e-14 ***
            8.476e-02 1.296e-02 6.542 6.81e-11 ***
UNTON
ED: EEM
            2.520e-02 6.868e-03
                                 3 669 0 000246 ***
Signif, codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.3519 on 4153 degrees of freedom Multiple R-squared: 0.4201, Adjusted R-squared: 0.4186

Multiple R-squared: 0.4201, Adjusted R-squared: 0.4186 F-statistic: 273.5 on 11 and 4153 DF, p-value: < 2.2e-16

Interactions with the * Operator

```
> reg_11 <- lm(LWAGE - ED*FEM + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
+ + MS + UNION, data = data)
> summarv(rea_11)
```

 This version gives us the interacted and uninteracted terms with one term.

```
Call:
lm(formula = LWAGE ~ ED * FEM + EXP + EXP2 + WKS + OCC + SOUTH +
   SMSA + MS + UNION, data = data)
Residuals:
    Min
              10 Median
-2.19425 -0.23540 -0.00569 0.23005 2.13574
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.277e+00 7.212e-02 73.173 < 2e-16 ***
FD
            5.413e-02 2.689e-03 20.126 < 2e-16 ***
FEM
           -7.153e-01 9.235e-02 -7.745 1.19e-14 ***
FXP
            4.053e-02 2.171e-03 18.668 < 2e-16 ***
EXP2
           -6.842e-04 4.776e-05 -14.324 < 2e-16 ***
WKS
            4.518e-03 1.088e-03 4.151 3.37e-05 ***
OCC
           -1.383e-01 1.472e-02 -9.396 < 2e-16 ***
SOUTH
           -7 375e-02 1 248e-02 -5 910 3 70e-09 ***
SMSA
           1.402e-01 1.206e-02 11.626 < 2e-16 ***
MS
            6.539e-02 2.061e-02 3.173 0.001520 **
            8.476e-02 1.296e-02
                                  6.542 6.81e-11 ***
UNTON
ED · EEM
            2 520e-02 6 868e-03 3 669 0 000246 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.3519 on 4153 degrees of freedom
Multiple R-sauared: 0.4201, Adjusted R-squared: 0.4186
```

F-statistic: 273.5 on 11 and 4153 DF. p-value: < 2.2e-16

4 D > 4 A > 4 B > 4 B > B 900

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Mincerian Regression: Sample Selection

- What happens when some of the data is missing in a non-random way?
- For example, let's imagine that the low-wage individuals drop out of the labor market.
- Note: this may already be happening in the data, but let's make it happen more.

```
> reg_7 <- lm(LMAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
+ MS + FEM + UNION, data = subset(data, LWAGE>=6))
> summary(reg_7)
```

```
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.609e+00 7.399e-02 75.805 < 2e-16 ***
            4.882e-02 2.569e-03 19.005 < 2e-16 ***
FXP
            3.199e-02 2.177e-03 14.694
EXP2
           -5.169e-04 4.801e-05 -10.766
WKS
            2.827e-03 1.106e-03
                                  2 556
occ
           -9.138e-02 1.435e-02 -6.369 2.12e-10 ***
SOUTH
           -5.565e-02 1.213e-02 -4.588 4.63e-06 ***
SMSA
            1.118e-01 1.165e-02
                                 9.596
MS
            9.364e-03 2.049e-02
                                  0.457
FEM
           -3.528e-01 2.625e-02 -13.439 < 2e-16 ***
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

2.012e-02 1.255e-02

Residual standard error: 0.3257 on 3833 degrees of freedom Multiple R-squared: 0.3148, Adjusted R-squared: 0.3131 F-statistic: 176.1 on 10 and 3833 DF, p-value: < 2.2e-16

 Recall that the coefficient on ED in the original regression was 5.654e-01

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Mincerian Regression: Measurement Error

- What happens if one of the variables of interest is measured with error?
- Let's say the the recorded education might be one year more or less than the person's actual education.
- Note: this may already be happening in the data, but let's make it happen more.

```
> noise <- sample(-1:1,dim(data)[1],replace=T)
> data <- chind(data, ED.NDISY-dataSED + noise)
> reg_8 <- lm(LMAGE - ED.NDISY + EXP + EXP2 + WKS + OCC + SOUTH + SMSA + KS + FEM + UNION, data = data)
> summary(reg_8)
```

```
Call:
lm(formula = LWAGE ~ ED_NOISY + EXP + EXP2 + WKS + OCC + SOUTH +
   SMSA + MS + FEM + UNION, data = data)
Residuals:
              10 Median
-2.23660 -0.23773 -0.00609 0.24132 2.09688
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.341e+00 7.094e-02 75.283 < 2e-16
ED NOTSY
            4.967e-02 2.451e-03 20.262 < 2e-16
            4.049e-02 2.188e-03 18.501 < 2e-16
FXP2
           -6.862e-04 4.813e-05 -14.257 < 2e-16
WKS
            4.618e-03 1.097e-03 4.209 2.62e-05
000
           -1.600e-01 1.457e-02 -10.977 < 2e-16 ***
SOUTH
           -7 690e-02 1 255e-02 -6 127 9 79e-10
SMSA
            1.435e-01 1.214e-02 11.825 < 2e-16
            6.591e-02 2.077e-02 3.174 0.00151
FFM
           -3.972e-01 2.533e-02 -15.683 < 2e-16
UNTON
            8.402e-02 1.295e-02 6.486 9.85e-11 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.3547 on 4154 degrees of freedom
```

F-statistic: 289.7 on 10 and 4154 DF. p-value: < 2.2e-16

 Recall that the coefficient on ED in the original regression was 5.654e-01

Adjusted R-squared: 0.4095

Multiple R-squared: 0.4109,

Omitted Variables Bias, Revisited

 Suppose the econometrician only observes regressors X, but the true model is

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{z}\gamma + \boldsymbol{\varepsilon},$$

The OLS estimator will equal

$$\mathbf{b} = \left(\mathbf{X}'\mathbf{X}\right)^{-1}\mathbf{X}'\mathbf{y} = \boldsymbol{\beta} + \left(\mathbf{X}'\mathbf{X}\right)^{-1}\mathbf{X}'\mathbf{z}\gamma + \left(\mathbf{X}'\mathbf{X}\right)^{-1}\mathbf{X}'\boldsymbol{\varepsilon}$$

- The last term is mean zero given the strict exogeneity assumption.
- Note that the second term will not be zero if $\bf X$ and $\bf z$ are correlated; i.e. if $\bf X'z \neq 0$.
- Implication: correlation between omitted variables and the observed regressors makes OLS biased.

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Omitted Variables Bias II

Using the Frisch-Waugh theorem, we can show that

$$E\left[b_{OLS,k}|\mathbf{X},\mathbf{z}\right] = \beta_k + \gamma \left(\frac{Cov\left(z,x_k|\mathbf{X}_{-k}\right)}{Var\left(x_k|\mathbf{X}_{-k}\right)}\right)$$

where \mathbf{X}_{-k} refers to all the regressors besides x_k .

- Suppose positive correlation between regressor x_k and omitted variable z.
- \bullet Also suppose $\beta_k>0$ and $\gamma>0$ so both variables have positive effects.
- Let's compare the average value of the dependent variable for $x_k=0$ and $x_k=1$. Two things change between these points:
 - ▶ Dependent variable Y increases by β_k because of direct effect of x_k .
 - Value of z should be higher because of the positive correlation between x_k and z. Higher values of z also contribute to a higher dependent variable because $\gamma > 0$.

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Omitted Variables Bias in Mincerian Regression

 What sort of variables might the wage equation omit, and how would you expect them to affect the estimated coefficients?

```
Call:
lm(formula = LWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA +
   MS + FEM + UNION, data = data)
Residuals:
   Min
            10 Median
-2.2034 -0.2379 -0.0071 0.2327 2.1380
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.245e+00 7.170e-02 73.153 < 2e-16
ED
            5.654e-02 2.612e-03 21.644 < 2e-16
EXP
            4.045e-02 2.174e-03 18.605 < 2e-16
FXP2
           -6.811e-04 4.783e-05 -14.242 < 2e-16
WKS
            4.485e-03 1.090e-03 4.115 3.94e-05
occ
           -1.405e-01 1.472e-02 -9.544 < 2e-16
SOUTH
           -7 210e-02 1 249e-02 -5 773 8 37e-09
SMSA
            1.390e-01 1.207e-02 11.513 < 2e-16
            6.736e-02 2.063e-02
                                  3.265
FFM
           -3.892e-01 2.518e-02 -15.457 < 2e-16 ***
            9.015e-02 1.289e-02
UNION
                                  6.993 3.13e-12 ***
Signif, codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.3524 on 4154 degrees of freedom
```

F-statistic: 298.7 on 10 and 4154 DF, p-value: < 2.2e-16

Adjusted R-squared: 0.4169

Multiple R-squared: 0.4183.

Outliers and Influential Observations

- Outliers refer to observations that are "far away" from the rest of the data. They can be due to errors in the data. There is no standard formal definition.
- **Influential Observations** refer to observations that have a large result on the estimated coefficients. Again, no standard definition.
- What to do? Greene: "It is difficult to draw firm general conclusions...
 It remains likely that in very small samples, some caution and close
 scrutiny of the data are called for." I'd say that's true even in large
 samples, but there isn't a generally accepted way of quantifying what
 counts as appropriate "caution and close scrutiny."
- Removing clear outliers from datasets is generally considered good practice (especially when such observations are likely errors).

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